

Tutorial 1

Exercise 1: Defining Semiconductors

In terms of electrical conductivity, describe where semiconductors sit relative to conductors and insulators. Explain how their conductivity responds to changes in temperature compared to metals.

Exercise 2: Categorizing Types

Contrast **Intrinsic** and **Extrinsic** semiconductors. Within extrinsic materials, explain the structural difference between an **n-type** and a **p-type** semiconductor, specifically mentioning the role of "dopants."

Exercise 3: Semiconductor Alloys

Define what a semiconductor alloy is and provide one example. Why would a manufacturer choose an alloy over a pure element like Silicon?

Exercise 4: Electron-Hole Dynamics

Describe the process of **Generation** (formation) and **Recombination** of electron-hole pairs. What external factor typically triggers the formation of these pairs in a dark environment?

Exercise 5: Energy Band Theory

Elucidate the concept of the **Energy Band Gap (E_g)**. Use this concept to explain why a diamond is an insulator while Silicon is a semiconductor.

Exercise 6: Describing Semiconductors

A Silicon (Si) sample at 300 K has an intrinsic carrier concentration $n_i \approx 1.5 \times 10^{10} \text{ cm}^{-3}$. Given the electron mobility $\mu_n = 1350 \text{ cm}^2/(\text{V} \cdot \text{s}^{-1})$ and hole mobility $\mu_p = 450 \text{ cm}^2/(\text{V} \cdot \text{s}^{-1})$, calculate the electrical conductivity σ of pure Silicon: $\sigma = n_i e (\mu_n + \mu_p)$

Exercise 7: Types of Semiconductors (Doping)

An n-type Silicon sample is doped with Phosphorus such that the donor concentration $N_D = 10^{16} \text{ cm}^{-3}$. If the intrinsic carrier concentration is $n_i = 1.5 \times 10^{10} \text{ cm}^{-3}$, determine the minority carrier (hole) concentration p_0 . Given the Mass action law: $n_0 \times p_0 = n_i^2$ and we assume that $n_0 \approx N_D$ at complete ionization

Exercise 8: Semiconductor Alloys

The bandgap E_g of the ternary alloy $\text{Al}_x\text{Ga}_{1-x}\text{As}$ at 300 K can be estimated using the Virtual Crystal Approximation for low x values. Calculate the bandgap for an alloy with 20% Aluminum ($x = 0.2$), given $E_g(\text{GaAs}) = 1.42 \text{ eV}$ and $E_g(\text{AlAs}) = 2.16 \text{ eV}$, $E_g(x) = xE_g(\text{AlAs}) + (1 - x)E_g(\text{GaAs})$

Exercise 9: Formation and Recombination

In a steady-state condition, light is shining on a semiconductor, creating excess electron-hole pairs (EHPs) at a generation rate $G = 10^{20} \text{ cm}^{-3} \text{ s}^{-1}$. If the minority carrier lifetime is $\tau = 10 \mu \text{ s}$, what is the steady-state excess carrier concentration Δn ? $\Delta n = G \times \tau$

Exercise 10: Energy Bands in Solids

The intrinsic carrier concentration n_i depends on temperature T and the bandgap E_g . If the temperature of a Silicon sample increases from 300 K to 350 K, how does the exponential term in the n_i formula change? (Assume $E_g = 1.12 \text{ eV}$ and $K_B = 8.617 \times 10^{-5} \text{ eV/K}$). and $n_i \propto \exp\left(\frac{-E_g}{2K_B T}\right)$

Exercise 11: Optoelectronic Sensor

An advanced materials laboratory is designing a high-sensitivity light sensor for a deep-space probe. To optimize the sensor for a specific deep-red wavelength (approx. 785 nm), the team uses a ternary alloy, $\text{Al}_x \text{Ga}_{1-x} \text{As}$, doped with Selenium (a donor impurity).

- Bandgap Engineering:** Determine the Aluminum mole fraction (x) required for the alloy to have a bandgap (E_g) corresponding to a 785 nm photon. (Use $(\text{eV}) = 1240/\lambda(\text{nm})$ and the alloy formula $E_g(x) = xE_g(\text{AlAs}) + (1-x)E_g(\text{GaAs})$, where $E_g(\text{GaAs}) = 1.42 \text{ eV}$ and $E_g(\text{AlAs}) = 2.16 \text{ eV}$).
- Doping & Conductivity:** The chosen alloy is then doped to create an n-type semiconductor with a donor concentration $N_D = 2 \times 10^{16} \text{ cm}^{-3}$. If the intrinsic carrier concentration n_i at the operating temperature is 10^6 cm^{-3} , calculate the minority carrier concentration (p_0).
- Steady-State Dynamics:** In a dark environment, the sensor is suddenly exposed to a laser, creating excess electron-hole pairs at a generation rate $G = 5 \times 10^{18} \text{ cm}^{-3} \text{ s}^{-1}$. If the minority carrier lifetime is $\tau = 2 \mu \text{ s}$, calculate the steady-state excess hole concentration Δp and the total hole concentration (p_{total} during illumination).
- Temperature Response:** If the probe moves closer to a star and the temperature increases, explain, using energy band theory, how this will affect the sensor's "dark current" (conductivity without light).